

AQA Further Maths AS-level Statistics

Formula Sheet

Provided in formula book

Not provided in formula book

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Discrete Random Variables and Expectation

Measures of Average and Spread for a Discrete Random Variable

Expectation	$E(X) = \sum_{i} x_i p_i$
Variance	$Var(X) = \sum_{i} x_{i}^{2} p_{i} - (E(X))^{2}$ $= E(X^{2}) - (E(X))^{2}$
Standard Deviation	$\sigma = \sqrt{Var(X)}$
Mode	The value of X which has the largest probability
Median	$P(X \le M) = 0.5$ $P(X \ge M) = 0.5$

Functions of Discrete Random Variables

$$E(aX + b) = aE(X) + b$$
$$Var(aX + b) = a^{2}Var(X)$$

Discrete Uniform Distribution

$$P(X = x) = \frac{1}{n} \text{ for } x = 1,2, \dots n$$

$$E(X) = \frac{n+1}{2}$$

$$Var(X) = \frac{n^2 - 1}{12}$$









Poisson Distribution

$$P(X = x) = e^{-\lambda} \frac{\lambda^{x}}{x!}$$

$$X \sim Po(\lambda)$$
Mean = λ

Variance = λ

Sum of Independent Poisson Distribution

When $X \sim Po(\lambda)$, $Y \sim Po(\mu)$ and Z = X + Y:

 $Z \sim Po(\lambda + \mu)$

Type I and Type II Errors

Defining Type I and Type II Errors

Type I Error H_0 is rejected when it is true

Type II Error H_0 is not rejected when it is false

In hypothesis testing:

significance level = $P(\text{type I error}) = P(\text{rejecting H}_0|\text{H}_0 \text{ is true})$











Continuous Random Variables

Probability Density Function (PDF)

For continuous random variable X with pdf f(x):

$$P(a < x < b) = \int_a^b f(x) \ dx$$

$$\int_{-\infty}^{\infty} f(x) \ dx = 1$$

$$f(x) \ge 0$$
 for all x

Median and Quartiles of a Given Probability Density Function

Lower quartile (Q_1)	$\int_{-\infty}^{Q_1} f(x) \ dx = \frac{1}{4}$
Median	$\int_{-\infty}^{M} f(x) \ dx = \frac{1}{2}$
Upper quartile (Q_3)	$\int_{-\infty}^{Q_3} f(x) \ dx = \frac{3}{4}$

Expectation and Variance of a Continuous Random Variable

$$E(X) = \int_{-\infty}^{\infty} x \, f(x) \, dx$$

$$E(X^2) = \int_{-\infty}^{\infty} x^2 f(x) \ dx$$

$$Var(X) = E(X^2) - (E(X))^2$$











Functions of a Continuous Random Variable

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$$E(aX + b) = aE(X) + b$$
$$Var(aX + b) = a^{2}Var(X)$$

General Function

$$E(g(X)) = \int_{-\infty}^{\infty} g(x)f(x) \ dx$$

Expectation and Variance of the Sum of Two Independent Random Variables

$$E(X + Y) = E(X) + E(Y)$$

$$Var(X + Y) = Var(X) + Var(Y)$$

Chi Squared Tests for Association

Chi squared Values and Degrees of Freedom

Expected frequency	$E_i = \frac{row \ total \times column \ total}{overall \ total}$
Chi squared value	$\chi_{calc}^2 = \sum_i \frac{(O_i - E_i)^2}{E_i}$
Degrees of freedom	$v = (no. of \ rows - 1)(no. of \ columns - 1)$

Condition on Expected Frequency

For
$$E_i > 5$$
:

$$\chi^2_{calc} \sim \chi^2_v$$

Confidence Intervals

Confidence interval for population mean μ

$$(\bar{x}-z\frac{\sigma}{\sqrt{n}},\bar{x}+z\frac{\sigma}{\sqrt{n}})$$

Width of confidence interval

$$2z\frac{\sigma}{\sqrt{n}}$$





